Silicon Photonics:

From Device Engineering to Large-Scale System Integration

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What is Silicon Photonics

Optical Technology



CMOS Fabrication Techniques



Images from Internet

Silicon Photonics

- Silicon (and other compatible materials) as the material for photonics
- Accessible to well-developed CMOS processing technology



Silicon Photonics: A Rich Device Library

Silicon Photonics Device Library



Silicon Photonic Devices

- High-refractive-index contrast: compact devices, integration
- Electro/Thermo-optic effects: active devices
- Hybrid integration: light sources



Silicon Photonics: From Devices to Systems



System Integration: A Unique Advantage of Si Photonics

• CMOS Compatibility: wafer-scale & nm-precision manufacturing; electronic-photonic integration; large scale (Moore's Law)



Silicon Photonics: From Devices to Systems



System Integration: A Unique Advantage of Si Photonics

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Integrated Optical Phased Array

- The ultra-compact unit cell
- Optical beam steering and manipulation



Arbitrary Beamform Generation

- Generating arbitrary beamforms: Gaussian, OAM, etc. OAM₊₄ OAM₋₄





Large-Scale Phased Array

- Optical phased array w/ up to 4,096 antennas - Largest silicon photonic circuit to date



Applications & Future Work

- LADAR, signal processing, communication, sensing, etc.

- Devices and materials



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The Unit Cell An 8 imes 8 Phased Array Faster and More Power Efficient

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The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Phased Array: A Well-Known Technology

F22 Raptor



PAVE PAWS: ALASKA



PAVE PAWS: CALIFORNIA





Phased Array: From Microwave to Lightwave

- Phased Array: beamshaping with an array of antennas
- Optical Phased Array: small $\lambda \rightarrow$ compact systems



Large-Scale Phased Array Arbitrary Beamform Generation Applications & Future Work The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Optical Phased Array: A Longer History



The Simplest Optical Phased Array

- Principle: interference & Fourier transform
- Antenna spacing: $d \sim \lambda \rightarrow$ opportunity for Si Photonics



The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Integrated Optical Phased Array: Previous Work



J. Doylend, et al, OE, 2011

K. van Acoleyan, et al, OE, 2010

Our Goal • Large-Scale: thousands ~ millions of antenna • Two-Dimensional: full control of the radiation field



The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Large-Scale Two-Dimensional Phased Array: Challenges



Break the Scaling-Up Limitation: Challenges

• Architecture: Parallel Feeding vs. Series Feeding

Jie Sun, et al, Nature, 493, pp. 195-199 (2013)



Silicon Photonics

The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Large-Scale Two-Dimensional Phased Array: Challenges



Series Feeding

Break the Scaling-Up Limitation: Challenges

- Architecture: Parallel Feeding vs. Series Feeding
- Ultra-Compact Unit Cell: Tunable Phase Shifter, Antenna, and Coupler

Jie Sun, et al, Nature, 493, pp. 195-199 (2013)



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Integrated Optical Phased Array Arbitrary Beamform Generation

The Unit Cell

Tunable Phase Shifter: Indirect vs. Direct Heating





Large-Scale Phased Array Arbitrary Beamform Generation Applications & Future Work The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Adiabatic Bend: Low-Loss Silicon Contact



Direct contact

Low-loss silicon contact

• Direct Contact: scattering loss



The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Adiabatic Bend: Low-Loss Silicon Contact



Direct contact



Adiabatic transition

Low-loss silicon contact

- Direct Contact: scattering loss
- Adiabatic: low loss

The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Adiabatic Bend: Low-Loss Silicon Contact





Jie Sun

The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Tunable Phase Shifter: Power & Speed







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12 / 47

Large-Scale Phased Array Arbitrary Beamform Generation Applications & Future Work

The Unit Cell An 8×8 Phased Array Faster and More Power Efficien

High-Efficiency Optical Emitter





The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

High-Efficiency Optical Emitter





High-Efficiency Optical Emitter

- Compact: $2.8\mu m \times 3.5\mu m \rightarrow Broadband$
- **Directionality:** Partial-Etch \rightarrow 51%[†], 35% \downarrow
- Anti-Reflection: $\Lambda < \lambda$

3.5 μm

Integrated Optical Phased Array Large-Scale Phased Array Arbitrary Beamform Generation

The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Directional Couplers



Large-Scale Phased Array Arbitrary Beamform Generation Applications & Future Work

The Unit Cell

Unit Cell Directional Coupler K(*L*) Pres Act(*L*) Unit Cell

The Unit Cell

- Size: 9μm×9μm
- Fabrication: 2 Dopings, 2 Metals

The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Top View



Cross Section





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Large-Scale Phased Array Arbitrary Beamform Generation Applications & Future Work The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

An 8×8 Phased Array



An 8×8 Phased Array

• Electrical Connections: 8×8 (Column)+8 (Row) = 72 heaters

Jie Sun, et al, Nature, 493, pp. 195-199 (2013)



Large-Scale Phased Array Arbitrary Beamform Generation Applications & Future Work The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Near- and Far-Field Measurement







Large-Scale Phased Array Arbitrary Beamform Generation Applications & Future Work The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Optical Beam Shaping



research Laboratory

Large-Scale Phased Array Arbitrary Beamform Generation Applications & Future Work The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Dynamic Optical Beam Shaping

Movie: Dynamic beam shaping

Optical Beam Shaping

• Thermal Efficiency: 8.5 mW per π phase shift per heater



Large-Scale Phased Array Arbitrary Beamform Generation Applications & Future Work The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Next: Faster, and Less Energy Consumption

Free-Carrier Plasma Dispersion Effect

- Pros: Fast (ns) & less Energy
- Cons: Very small effect



The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Next: Faster, and Less Energy Consumption





The Unit Cell An 8×8 Phased Array Faster and More Power Efficient

Next: Faster, and Less Energy Consumption







Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Integrated Optical Phased Array

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- Generating arbitrary beamforms: Gaussian, OAM, etc. OAM₊₄ OAM₋₄



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Large-Scale Phased Array Arbitrary Beamform Generation

Phased Array Synthesis

Large-Scale Phased Array: Motivation





Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Large-Scale Phased Array Synthesis



Large-Scale Phased Array Synthesis

- Approach: Fourier transform w/ a constraint (uniform near-field intensity)
- Example: 64×64
- Performance: fast convergence



Silicon Photonics

Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Large-Scale Phased Array Synthesis

Movie: Large-Scale Phased Array Synthesis

Large-Scale Phased Array Synthesis

- Approach: Fourier transform w/ a constraint (uniform near-field intensity)
- Example: 64×64
- Performance: fast convergence



Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Implementation: A Large-Scale Si-Photonic PIC



Large-Scale Optical Phased Array

• Phase: 'hard-coded' in the unit cell, φ_{mn}



Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Fabricated Large-Scale Optical Phased Array



Phased Array

Unit Cell

CMOS-Compatible Si Photonic Process Unit Cell: 9μm×9μm (multiple times of operating λ = 1.55μm) Phased Array System: 0.576mm×0.576mm (64×64)



Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Near Field Measurement



research Laboratory of electronics AT MI

Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Near Field Measurement



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Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Near Field Measurement



Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Far Field Measurement





Far Field

- Result: 4,096 unit cells, 12,288 Si-Photonic components
- Impact: Largest (Optical) Phased Array & Si PIC; Power of Si-Photonics

The RESEARCH LABORATORY OF ELECTRONICS AT MIT Jie Sun, et al, *Nature*, **493**, pp. 195-199 (2013) Silicon Photonics 2

Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Far Field Measurement



Far Field

- Result: 4,096 unit cells, 12,288 Si-Photonic components
- Impact: Largest (Optical) Phased Array & Si PIC; Power of Si-Photonics



Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Toward Reconfigurable Large-Scale Optical Phased Array





Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Toward Reconfigurable Large-Scale Optical Phased Array



Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Toward Reconfigurable Large-Scale Optical Phased Array





Phased Array Synthesis Implementation and Measurements Toward 3D Electronic-Photonic Integration

Electronic-Photonic 3D Integration





Integrated Optical Phased Array Large-Scale Phased Array Arbitrary Beamform Generation

Toward 3D Electronic-Photonic Integration

Fabricated Photonics



Heaters 3D Via 5 um

Phased Array

Unit Cell

Electronic-Photonic Integration Photonics: 32×32 phased array, $20 \mu m$ unit cell size **Electronics:** Δ - Σ circuit (under development) Integration: Challenging, but promising



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Gaussian Beam Generation Optical Vortex Beam

Integrated Optical Phased Array

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Gaussian Beam Generation Optical Vortex Beam

Arbitrary Beamform Generation: Principle



Gaussian Beam Generation Optical Vortex Beam

Arbitrary Beamform Generation: Principle



Gaussian Beam Generation Optical Vortex Beam

Example: Generating A Gaussian Beam



Gaussian Beam Array



Jie Sun, et al, CLEO Postdeadline, San Jose, 2013



Gaussian Beam Generation Optical Vortex Beam

Example: Generating A Gaussian Beam



Jie Sun, et al, CLEO Postdeadline, San Jose, 2013

Near field Far field

Uniform Arrav





Gaussian Beam Generation Optical Vortex Beam

Example: Generating A Gaussian Beam



Gaussian Beam Array



Jie Sun, et al, CLEO Postdeadline, San Jose, 2013



Gaussian Beam Generation Optical Vortex Beam

Dynamic Beam Manipulation





Gaussian Beam Generation Optical Vortex Beam

Optical Vortex Beam: A Twist of Light





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Wavefront of an OAM_{+4} Beam

Optical Vortex/ Orbital Angular Momentum (OAM)

 Definition: E ~ exp(j · l · θ) l ∈ Z: topological charge, OAM: L = lħ

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Gaussian Beam Generation Optical Vortex Beam

Optical Vortex Beam: A Twist of Light





J. E. Curtis & D. G. Grier, PRL, 90, 2003

Optical Vortex/ Orbital Angular Momentum (OAM)

- Definition: E ~ exp(j · l · θ)
 l ∈ ℤ: topological charge, OAM: L = lħ
- Applications:
 - Optical trapping

Gaussian Beam Generation Optical Vortex Beam

Optical Vortex Beam: A Twist of Light





A. E. Willner, et al, Nat. Photon., 6, 488-96, 2012

Optical Vortex/ Orbital Angular Momentum (OAM)

- **Definition:** $E \sim \exp(j \cdot l \cdot \theta)$
 - $l \in \mathbb{Z}$: topological charge, OAM: $L = l\hbar$
- Applications:
 - Optical trapping
- Optical space division multiplexing

Gaussian Beam Generation Optical Vortex Beam

Optical Vortex Beam: A Twist of Light





N. Bozinovic, et al, Science, 340, 1545-48, 2013

Optical Vortex/ Orbital Angular Momentum (OAM)

- Definition: E ~ exp(j · l · θ)
 l ∈ ℤ: topological charge, OAM: L = lħ
- Applications:
 - Optical trapping
- Optical space division multiplexing

Gaussian Beam Generation Optical Vortex Beam

Generating OAM: An Integrated Silicon Photonic Solution





Gaussian Beam Generation Optical Vortex Beam

Generating OAM: An Integrated Silicon Photonic Solution





Gaussian Beam Generation Optical Vortex Beam

Generating OAM: An Integrated Silicon Photonic Solution



Near-field Intensity





Gaussian Beam Generation Optical Vortex Beam

Generating OAM: An Integrated Silicon Photonic Solution



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Gaussian Beam Generation Optical Vortex Beam

Generating OAM: An Integrated Silicon Photonic Solution



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Gaussian Beam Generation Optical Vortex Beam

Generating OAM: An Integrated Silicon Photonic Solution



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Gaussian Beam Generation Optical Vortex Beam

Detecting Topological Charge *l*

OAM+4



OAM_4





Gaussian Beam Generation Optical Vortex Beam

Detecting Topological Charge *l*



Gaussian Beam Generation Optical Vortex Beam

Detecting Topological Charge *l*







Gaussian Beam Generation Optical Vortex Beam

Detecting Topological Charge *l*





Q: How to interfere two beams?

Gaussian Beam Generation Optical Vortex Beam

Detecting Topological Charge *l*





Q: How to interfere two beams?

• Thorlabs Solution: Free space

Gaussian Beam Generation Optical Vortex Beam

Detecting Topological Charge *l*





Q: How to interfere two beams?

- Thorlabs Solution: Free space ...
- Our Solution: Silicon photonics!

Gaussian Beam Generation Optical Vortex Beam





Gaussian Beam Generation Optical Vortex Beam







Gaussian Beam Generation Optical Vortex Beam







Gaussian Beam Generation Optical Vortex Beam









Gaussian Beam Generation Optical Vortex Beam

Interference at An Angle

Interference w/ an angle




Arbitrary Beamform Generation

Optical Vortex Beam

Interference at An Angle

Interference w/ an angle





Arbitrary Beamform Generation

Optical Vortex Beam

Interference at An Angle

Interference w/ an angle





Gaussian Beam Generation Optical Vortex Beam

Application: Space Division Multiplexing

Space Division Multiplexing





Gaussian Beam Generation Optical Vortex Beam

Next: Toward OAM w/ Reconfigurable Topological Charge l



Tunable OAM

- Motivation: Space division multiplexing, etc.
- Circular Array: $\theta = m \cdot \Delta \theta$
- Tunable Phase Shifter: $\Delta \varphi(V)$
- Emitting Field: $E \sim e^{j \cdot m \Delta \varphi(V)}$ when $\Delta \varphi(V) = l \cdot \Delta \theta \rightarrow E \sim e^{j \cdot l(m \Delta \theta)} = e^{j \cdot l \theta}$

Tunable Phase Shifter



Circular Antenna Array





Gaussian Beam Generation Optical Vortex Beam

Reconfigurable OAM: Simulation



Reconfigurable OAM

• Inline Heater: to change topological charge $l = \frac{\Delta \varphi(V)}{\Delta \theta}$



Gaussian Beam Generation Optical Vortex Beam

Reconfigurable OAM: Simulation



Reconfigurable OAM

- Inline Heater: to change topological charge l = Δφ(V)/Λθ
- Pre-Line Heater: to visualize the spiral wavefront



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Arbitrary Beamform Generation

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Optical Phased Array Communication and Computation Optical/Microwave Signal Processing Devices and Materials

Large-Scale Phased Array

Optical phased array w/ up to 4,096 antennas
 Largest silicon photonic circuit to date



Applications & Future Work

- LADAR, signal processing, communication, sensing, etc.

- Devices and materials





Optical Phased Array

Faster & Lower Power

Larger & More Controllable

Optical Phased Array

Applications











Images a, b, and c from Internet



Optical Phased Array Communication and Computation Optical/Microwave Signal Processing Devices and Materials

$\textbf{Telecom}{\rightarrow} \textbf{Datacom}{\rightarrow} \textbf{Intrachip}$





Optical Phased Array Communication and Computation **Optical/Microwave Signal Processing** Devices and Materials

Optical Arbitrary Waveform Generation & Microwave Photonics



Optical/Microwave Signal Processing

- Optical AWG: delay and/or reshape optical pulses
- Microwave Photonics: generation and manipulation of RF signals using integrated photonics



Optical Phased Array Communication and Computation Optical/Microwave Signal Processing Devices and Materials

Backbones of Silicon Photonics: Materials & Devices



Optical Phased Array Communication and Computation Optical/Microwave Signal Processing Devices and Materials

Bragg Grating Array with Highly-Uniform Channel Spacing



• Integration with III-V gain for WDM



Jie Sun, et al, Opt. Lett., 38, pp. 4002-04 (2013)

Bright Future of Silicon Photonics

Optical Technology



CMOS Fabrication Techniques



Images from Internet

Silicon Photonics

- Silicon (and other compatible materials) as the material for photonics
- Accessible to well-developed CMOS processing technology



Backup Slides

- Silicon Photonic Devices

 Sampled Bragg Grating
 A Thermo-Optic Switch

 Silicon Photonic Process
 Phased Array Related
 - An Ultra-Small Bend
 - High-Order Interference
 - Phase/Intensity Noise in Phased Array
 - Continuously Steerable Phased Array

4 OAM Related

• Polarization of Tunable OAM



Sampled Bragg Grating A Thermo-Optic Switch

$\lambda/4$ -Shifted Bragg Grating Enabled by Sampling



$\lambda/4$ -shifted Bragg grating enabled by sampling

- Phase shift: $\Delta \phi = 2\pi \frac{\Delta L_2}{P}$ (Quarter-Wave: $\Delta \phi = \pi \rightarrow \Delta L_2 = \frac{P}{2}$)
- $P \sim 100 \mu m$, $\Delta L_2 \sim 50 \mu m \rightarrow$ Easy fabrication!

Sampled Bragg Grating A Thermo-Optic Switch

$\lambda/4$ -shifted Bragg Grating Enabled by Sampling



Relaxed fabrication requirement yet improved accuracy

• Interference lithography + contact lithography (1µm-resolution)

Jie Sun, C. W. Holzwarth, and H. I. Smith, IEEE PTL, 24, pp. 25-27 (2012)



Silicon Photonic Devices

OAM Related

Sampled Bragg Grating A Thermo-Optic Switch

An Optical Switch (Power Consumption P_{π})





Sampled Bragg Grating A Thermo-Optic Switch

An Optical Switch (Power Consumption P_{π})





An optical switch enabled by tunable phase shifter

- Light-doping: large resistance, low optical loss
- Heavy-doping: small resistance
- Long contact line: thermal isolation

Sampled Bragg Grating A Thermo-Optic Switch

An Optical Switch (Power Consumption P_{π})





Silicon Photonic Devices

licon Photonic Process Phased Array Related OAM Related Sampled Bragg Grating A Thermo-Optic Switch

An Optical Switch (Response Time τ)





Silicon Photonics

Fabrication: The CMOS-Compatible Si-Photonic Process



A customized CMOS-compatible Si-photonic process

- 300-mm SOI (220nm Si, 2μm BOX) line at 65-nm node using 193-nm optical immersion lithography
- Si (2 etches, 4 doping levels), 2 metal interconnections, Ge, SiNx, Er³⁺ (backend processing)



An Ultra-Small Bend High-Order Interference Phase/Intensity Noise in Phased Array Continuously Steerable Phased Array

A Ultra-Small Bend (2 μm)





Jie Sun

An Ultra-Small Bend High-Order Interference Phase/Intensity Noise in Phased Array Continuously Steerable Phased Array

A Ultra-Small Bend (2 μm)





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An Ultra-Small Bend High-Order Interference Phase/Intensity Noise in Phased Array Continuously Steerable Phased Array

High-Order Interference



Jie Sun, et al, IEEE JSTQE, 20(4), 2014



An Ultra-Small Bend High-Order Interference Phase/Intensity Noise in Phased Array Continuously Steerable Phased Array

Phase/Intensity Noise Tolerance



An Ultra-Small Bend High-Order Interference Phase/Intensity Noise in Phased Array Continuously Steerable Phased Array

Phase/Intensity Noise Tolerance



Jie Sun, et al, IEEE JSTQE, 20(4), 2014



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An Ultra-Small Bend High-Order Interference Phase/Intensity Noise in Phased Array Continuously Steerable Phased Array

Phase/Intensity Noise Tolerance



Silicon Photonic Devices An Ultra-Small Bend Silicon Photonic Process High-Order Interference Phased Array Related Continuously Steerable Phased Array

Continuously Steerable Phased Array



Continuously steerable

- Linear phase: $\varphi_m = m \cdot \frac{\sin(\theta)\Delta x}{k}$ θ : steering angle
- In-line phase shifter: simplified electrical control

Silicon Photonic Devices An Ultra-Small Bend Silicon Photonic Process High-Order Interference Phased Array Related Continuously Steerable Phased Array

Continuously Steerable Phased Array





An Ultra-Small Bend High-Order Interference Phase/Intensity Noise in Phased Array Continuously Steerable Phased Array

Fabricated Continuously Steerable Phased Array



Unit Cell



Continuously steerable array w/ inline heaters

• Unit cell: 16µm×16µm (5.6°, can be improved)

An Ultra-Small Bend High-Order Interference Phase/Intensity Noise in Phased Array Continuously Steerable Phased Array

Fabricated Continuously Steerable Phased Array

Continuously Tunable Phased Array



Unit Cell



Continueous Beam Steering



Continuously steerable array w/ inline heaters

- Unit cell: 16µm×16µm (5.6°, can be improved)
- Efficiency: 16.9mW per 2π phase shift per heater

An Ultra-Small Bend High-Order Interference Phase/Intensity Noise in Phased Array Continuously Steerable Phased Array

Fabricated Continuously Steerable Phased Array

Continuously Tunable Phased Array



Unit Cell



Continueous Beam Steering



• Speed: several tens of μs

Polarization of Tunable OAM

Polarization of Circular Array



Polarization of The Antenna Emission

•
$$\vec{E} = \begin{pmatrix} -\sin\theta\\\cos\theta \end{pmatrix} \cdot e^{j \cdot l\theta} = \frac{-j}{2} \left(e^{j(l-1)\theta} \cdot \begin{pmatrix} 1\\j \end{pmatrix} + e^{j(l+1)\theta} \cdot \begin{pmatrix} 1\\-j \end{pmatrix} \right)$$

• LHCP $(l-1)$ + RHCP $(l+1)$

